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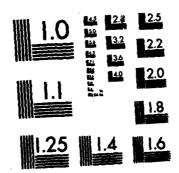
MODEL REFERENCE ADAPTIVE CONTROL SYSTEMS: THE HYBRID APPROACH(U) MASSACHUSETTS UNIV AMHERST DEPT OF ELECTRICAL AND COMPUTER EN. R CRISTI ET AL. JUL 82

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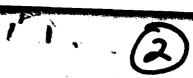
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4. TITLE (and Subtitio) MODEL REFERENCE ADAPTIVE CONTROL SYSTEMS: THE	8. Type of Report & Period Covered TECHNICAL
HYBRID APPROACH	6. PERFORMING ORG. REPORT NUMBER
7. AUTHOR(a)	WA2 - 10:15 6. CONTRACT OR GRANT NUMBER(s)
R. Cristi and R.V. Monopoli	AFOSR-80-0155
9. PERFORMING ORGANIZATION NAME AND ADDRESS Electrical & Computer Engineering Department University of Massachusetts Amherst MA 01003	10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS PE61102F; 2304/A1
11. CONTROLLING OFFICE NAME AND ADDRESS Directorate of Mathematical & Information Sciences Air Force Office of Scientific Research	12. REPORT DATE JULY 1982
Bolling AFB DC 20332	13. NUMBER OF PAGES S
14. MONITORING AGENCY NAME & ADDRESS(II different from Controlling Office)	UNCLASSIFIED 15a. DECLASSIFICATION/DOWNGRADING SCHEDULE
16. DISTRIBUTION STATEMENT (of this Report) Approved for public release; distribution unlimited	DTIC ELECTED NOV 1 5 1982

17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)

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18. SUPPLEMENTARY NOTES

19. KEY WORDS (Continue on reverse side if necessary and identity by block number)

ABSTRACT (Continue on reverse side if necessary and identity by block number)

In this report, an algorithm for adaptive control of continuous time singleinput single-output systems is presented. With the hybrid approach, the control structure involves a continuous as well as a discrete time part, instead of being totally discrete or totally continuous as in previous approaches. The system is sampled and the adaptive gains updated at a variable rate varying with the magnitude of the error itself.

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MODEL REFERENCE ADAPTIVE CONTROL SYSTEMS: THE HYBRID APPROACH

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In this report, an algorithm for adaptive control of continuous time single-input single-output systems is presented. With the hybrid approach, the control structure involves a continuous as well as a discrete time part, instead of being totally discrete or totally continuous as in previous approaches.

The system is sampled and the adaptive gains updated at a variable rate varying with the magnitude of the error itself.

Introduction

The theory and application of Adaptive Control Systems have been a center of discussion in the last few years. Continuous-time [1], [6], [7], [8], as well as discrete-time [2], [5], [9], [10] schemes have been devised, and stability has been proved.

In spite of the continuous-time nature of real systems, from a point of view of applications, discrete-time algorithms are preferred to continuous-time, due to recent advances in digital technology.

However, the discrete approach is not closely coupled to the continuous-time behavior of real plants, making a "hybrid" approach (partly discrete, partly continuous) desirable. It is a well known result [1], [6], that, for a given plant, poles and zeroes can be arbitrarily placed with appropriate compensators as in Fig. 1. If the plant parameters are known exactly, then the control input which gives the desired behavior is of the form

u(t) = K^{*T} $\underline{\phi}(t)$, $\underline{\phi}(t)$ being filtered versions of the plant input and output, and K^* an array of constants. In case of plant unknown, or partially known, the input assumes the form

input assumes the form $u(t) = K(t)^{-1} y(t)$, where $K(t) = K(t)^{-1} y(t)$, where $K(t) = K(t)^{-1} y(t)$. In the hybrid scheme which will be the subject of this paper, the set of parameters K(t) are updated by a digital computer at discrete intervals of time $\{t_k\}$, and the continuous-time nature of u(t) is preserved. The overall scheme of the control system is

The overall scheme of the control system is shown in Fig. 2.

Recently, hybrid algorithms for adaptive

control [4] as well as self-tuning regulators [11], have been devised. In [4] the adaptive gains $\underline{K}(t)$ are discretely updated at a fixed rate, in base of samples taken from the plant in a random fashion.

It turns out that the sampling scheme is crucial in order to establish stability of the closed loop system. In this paper, the system is sampled, and the adaptive gains updated, at a variable rate according to the magnitude of the continuous time error itself. It is shown that the continuous time error becomes smaller than any bound, arbitrarily determined, after a finite number of adaptation steps.

The problem is stated in Section 1, with the error model in Section 2. The adaptive law is discussed in Section 3, and Section 4 describes the sampling scheme, with proof of stability.

Notation

The following notation will be used:

- vectors: a = [a1, a2, ..., an];

- time delay operator: Z;

- differential operator: p = d

 x(t) = O[y(t)] iff there exists a positive constant N such that |x(t)| ≤ N|y(t)|, for any t;

for any t; - x(t) = o[y(t)] iff |x(t)| < a(t)|y(t)|for some function a(t) such that a(t)-0;

-x(t) - y(t) iff x(t) = 0[y(t)] and y(t) = 0[x(t)];

- L'denotes Liplace Transform operation.

1. Statement of the Problem

A continuous time dynamic system (plant) can be described by the linear time invariant, non-autonomous differential equation

(1.1) $D_p(p) \times (t) = D_p(p) \cdot u(t)$ with $D_p(p) = p^n + a_1 p^{n-1} + ... + a_n$

 $D_{\alpha}(p) = b_0 p^m + b_1 p^{m-1} + \dots + b_m$ The following assumptions are made on the

plant parameters: (1) the values of a , 1-1, ..., n and b4, 1-0,

.... m, are unknown:

(ii) m < n-1 is known; (iii) the plant is minimum phase; i.e., the polynomial $D_{u}(p)$ is Hurwitz;

(1v) the sign of bo is known, as are bounds both

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and b_{OM} , where $b_{OM} \geq b_{O} \geq b_{OM}$. Without loss of generality, $b_{OM} > 0$ will be

Given a mode) (1.2) $D_{m}(p) \times_{m}(t) = K_{0}r(t)$, with $D_{m}(n) = pn + a_{m}pn-1 + ... + a_{mn}$, Hurwitz, the design objective is to determine an input to the plant u(t) such that, for some $E_0>0$, tr>0(1.3) $|e(t)| \le E_0$, for every $t \ge tF$, where

(1.3') e(t) 4 xm(t) - x(t) In particular, we restrict the input u(t) to be of the form (1.4) $u(t) = \sum_{k=1}^{\infty} K_i(k) + i(t)$, for $t \in [t_k, t_{k+1}]$

where K (k), i=1, 2, ... n is a set of gains updated only at discrete instants $\{t_k\}$, and $\psi_i(t)$ are continuous time, observable state variables of the system.

2. The Error Model

It has been shown in [1] that constant

vectors \underline{a}_{ij} and \underline{a}_{ij} exist such that (2.1) $\underline{0}_{ij}(p)e(t) = \underline{0}_{ij}(p)[-b_0uf(t) + \underline{a}_{ij}]\underline{a}_{ij}(t) +$ $g_{x}^{T}g_{x}(t) + K_{0}g_{0}(t)$

where the following definitions pertain: $- O_M(p) + p^{n-1} + C_1 p^{n-2} + \ldots + C_{n-1} \text{ is a}$

Hurwitz polynomial such that $D_{\mathbf{w}}(\mathbf{p})$ is Strictly

Positive Real (S.P.R.); - $u_f(t)$ is such that $O_f(p)u_f(t) = u(t)$ where $\begin{array}{lll} D_f(p) &= p^{n-m-1} + F_1p^{n-m-2} + \ldots + F_{n-m-1} \text{ is any} \\ \text{Hurwitz polynomial of degree } n-m-1; \\ &= -\psi_1^{-1}(t), \ i=0, \ldots, n-2 \text{ are solutions of} \\ U_g(p)U_f(p)\psi_1^{-1}(t) &= p^{-1}u(t); \\ &= -\psi_1^{-1}(t), \ i=0, \ldots, n-1 \text{ are solutions of} \\ U_g(p)U_f(p)\psi_2^{-1}(t) &= p^{-1}x(t); \\ &= -\psi_1^{-1}(t), \ i=0, \ldots, n-1 \text{ are solutions of} \\ U_g(p)U_f(p)\psi_2^{-1}(t) &= p^{-1}x(t); \\ &= -\psi_1^{-1}(t), \ i=0, \ldots, n-1 \text{ are solutions of} \\ U_g(p)U_f(p)\psi_2^{-1}(t) &= -\psi_1^{-1}(t), \ i=0, \ldots, n-1 \text{ are solutions of} \\ U_g(p)U_f(p)\psi_2^{-1}(t) &= -\psi_1^{-1}(t), \ i=0, \ldots, n-1 \text{ are solutions of} \\ U_g(p)U_f(p)\psi_2^{-1}(t) &= -\psi_1^{-1}(t), \ i=0, \ldots, n-1 \text{ are solutions of} \\ U_g(p)U_f(p)\psi_2^{-1}(t) &= -\psi_1^{-1}(t), \ i=0, \ldots, n-1 \text{ are solutions of} \\ U_g(p)U_f(p)\psi_2^{-1}(t) &= -\psi_1^{-1}(t), \ i=0, \ldots, n-1 \text{ are solutions of} \\ U_g(p)U_f(p)\psi_2^{-1}(t) &= -\psi_1^{-1}(t), \ i=0, \ldots, n-1 \text{ are solutions of} \\ U_g(p)U_f(p)\psi_2^{-1}(t) &= -\psi_1^{-1}(t), \ i=0, \ldots, n-1 \text{ are solutions of} \\ U_g(p)U_f(p)\psi_2^{-1}(t) &= -\psi_1^{-1}(t), \ i=0, \ldots, n-1 \text{ are solutions of} \\ U_g(p)U_f(p)\psi_2^{-1}(t) &= -\psi_1^{-1}(t), \ i=0, \ldots, n-1 \text{ are solutions} \\ U_g(p)U_f(p)\psi_2^{-1}(t) &= -\psi_1^{-1}(t), \ i=0, \ldots, n-1 \text{ are solutions} \\ U_g(p)U_f(p)\psi_2^{-1}(t) &= -\psi_1^{-1}(t), \ i=0, \ldots, n-1 \text{ are solutions} \\ U_g(p)U_f(p)\psi_2^{-1}(t) &= -\psi_1^{-1}(t), \ i=0, \ldots, n-1 \text{ are solutions} \\ U_g(p)U_f(p)\psi_2^{-1}(t) &= -\psi_1^{-1}(t), \ i=0, \ldots, n-1 \text{ are solutions} \\ U_g(p)U_f(p)\psi_2^{-1}(t) &= -\psi_1^{-1}(t), \ i=0, \ldots, n-1 \text{ are solutions} \\ U_g(p)U_f(p)\psi_2^{-1}(p)$

- $\phi_0(t)$ is solution of $B_{\mu}(p)\phi_0(t) = r(t)$.

If we choose $O_{\mathbf{p}}(\mathbf{p}) = (\mathbf{p}+\mathbf{a})O_{\mathbf{p}}(\mathbf{p})$, with $\mathbf{a} > 0$, a

nce $\{t_k\}$, and $\{2.2\}$ up(t) = $K_{ij}^{T}(k) \underline{A}_{ij}(t) + K_{ij}^{T}(k) \underline{A}_{ij}(t) +$

 $K_0(k)\phi_0(t)+w_1(t)$, for $te[t_k,\,t_{k+1})$, we can write (2.1) as (2.3) $(p+u)e(t)=\frac{e}{2} (k) \frac{1}{2} (k) \frac{1$

 $\begin{array}{c} \xi_0(k)\phi_0(t) = b_0 \omega_1(t), \ \ \text{for te}[t_k,\ t_{k+1})\\ \text{where } g_1(k) \stackrel{\text{d}}{=} K_1(k) = b_0 g_1,\ j=u,x,o. \end{array}$ In what follows, the sequences $K_1(k)$ will be called the Adaptive Gains, and will be updated at the sampling instants $\{t_k\}$ only. Furthermore, the input u(t) has to be determined such that $\{1.3\}$ is

input u(t) new satisfied.

If (2.3) is sampled at instants $\{t_k\}$, the samples of the error are related by the linear, time variant difference equation (2.4) $e(t_k) = A_k e(t_{k-1}) + \frac{1}{2} (k-1) \frac{2}{2} (k) + \frac{1}{2} (k) + \frac{1}{2} (k-1) \frac{2}{2} (k) + \frac{1}{2} (k)$

 $T_k = t_k - t_{k-1};$ $A_k = \exp(-\epsilon T_k);$

(2.5) $\underline{i}_{1}(k) = \underline{e}_{1}(e_{k}) - A_{k-1} \underline{e}_{1}(e_{k-1}),$ ix,u,0 - L

(p+a)
$$\xi_{j}(t) = \underline{t}_{j}(t)$$
, $j = 0.u.x$;
 $u_{j}(k) = \int_{t_{k-1}}^{t_{k}} \exp -a(t_{k}-\tau)w_{j}(\tau)d(\tau)$

Introducing the auxiliary network (2.6) $y(k) = A_k y(k-1) + q(k) + w(k)$ with $\eta(k) \triangleq e(t_k) + y(k)$, equations (2.4) and

(2.6) yield (2.7) $\eta(k) = A_k \eta(k-1) + \underline{g}^T(k-1) \underline{\bar{g}}(k) + w(k) - b_0 \bar{g}^T(k) + q(k)$

(2.8) $\frac{d^{T}(k)}{d^{T}(k)} \stackrel{\triangle}{=} \left[\frac{d_{H}}{d^{T}}(k)\right]$ 6, T(k) 6₀(k)];

Let us choose

(2.9) $w(k) = K_w(k-1)\hat{w}_1(k)$, (2.7) becomes (2.10) $n(k) = A_k(k-1) + e^{T}(k-1) - \frac{1}{2}(k) + \frac{1}{2}(k-1) - \frac{1}{2}(k)$ $\delta_{\mathbf{k}}(\mathbf{k}-1)\tilde{\mathbf{w}}_{1}(\mathbf{k})+q(\tilde{\mathbf{k}}),$

which is the augmented error equation.

3. Adaptive Law

The equations in the previous section hold for any sampling sequence $\{t_k\}$, on which no hypothesis has been made so far.

introductions has been made so far.

If we suppose $\{t_k\}$ be a sequence with an infinite number of elements, then it is a well known result—[2], [3]—that equation (2.10) and the following adaptive law $\{3.7\}$ $\frac{d}{d}(k) = \frac{d}{d}(k-1) - \frac{d}{d}(k) = \frac{d}{d}(k)$

$$\delta_{M}(k) = \delta_{M}(k-1) + \frac{1}{\lambda_{1}} \tilde{w}_{1}(k) n(k)$$

 $F = \text{diag}(\frac{1}{\lambda_{1}}, 1 = \tilde{1}, N), y > 1/2 \min(\lambda_{1}, \lambda_{M}),$

with $F = \text{diag} \left(\frac{1}{\lambda_1}\right)$

Y₁, Y_N > 0, yield $\{\underline{e}(k)\}$ be a uniformly bounded sequence, and moreover (3.2) lim n(k) = 0

(3.3)
$$\lim_{k \to \infty} \underline{\vec{k}}(k) \eta(k) = 0$$

Let us define the cogtrol input as $(3.4) \quad u(t) = \underbrace{K}(k) \quad \phi(t), \quad t \in [t_k, t_{k+1})$

(3.5) $\underline{\bullet}(t) = 0e(n-n-1) \underline{\bullet}(t);$ equations (3.4) and (2.2) then yield
(3.6) $w_1(t) = u_2(t) - K^T(k) \underline{\bullet}(t),$

t e [tk, tk+]). which, together with (2.5), gives the remaining input to the auxiliary network (3.7) $\tilde{n}_{\parallel}(k) = \tilde{n}_{\parallel}(k) - K^{\parallel}(k-1) \tilde{\underline{s}}(k)$

 c_k sup $-a(c_{k}-r)$ $u_f(r)$ dr.

Stability and Sampling School

A suitable choice of the sampling sequence $\{t_k\}$ is crucial to prove stability of the closed loop system. It is evident, in fact, from $\{2,1\}$ that if the output of the plant grows without bound in an oscillating fashion, we might choose $\{t_k\}$ such that $\eta(k)=0$ for every k, and the seins never be updated.

A sufficient requirement on the sampling wence can be stated as follows: Theorem 4.1. Let the sampling sequence $\{t_k\}$ have an infinite number of terms, and be such that $\{4.1\}$ sup $[e(s)] = 0[\sup\{e(t_n)\}]$.

Then the hybrid system described in the previous sections is uniformly stable and (4.2) lim $e(t_k) = 0$

Proof: see [12].

The central idea contained in Theorem 4.1 is that stability of the overall system is guaranteed if the sampled error {e(tk)} grows at the same rate as the continuous time error itself—as stated in (4.1).

Notice that the random sampling scheme discussed in [4] satisfies (4.1)—as in [4, lem 2]—and then can be implemented to obtain stability in an almost sure sense.

In what follows a variable rate sampling scheme will be discussed, in which the sampling instants are determined by the comparison of a filtened wavelen of the among with the among

filtered version of the error with the error itself.

Let c(.) be such that

(4.3)
$$e(t) \stackrel{d}{=} c_0 \int_0^t e^{-\lambda(t-\tau)} |e(\tau)| d\tau$$

(4.4) $0 < c_0 < \lambda < \text{Re}[\alpha_1]$, $i=1, \ldots, 2n-1$, and $\{\alpha_1, i=1, 2n-1\}$ being the zeroes of the Huryftz polynomial $O_m(s)O_F(s)O_U(s)$. Then the following can be proved: Theorem 4.2. If the sampling sequence $\{t_k\}$ is chosen such that

(4.5) $t_{k+1} = \min \{\tau | |e(\tau)| \ge \max \{E_0, e(\tau)\}\}$ 726k+1

with Eq. T arbitrary positive constants, and $\epsilon(\cdot)$ as in (4.3), then the Hybrid Adaptive Control m discussed in the previous sections has the following properties:

the error |e(·)| is uniformly bounded;
 the sampling sequence (t_k) is a finite

an instant to exists such that $(4.6) |e(t)| \le E_0$, for every $t \ge t_F$.

Sefere going into the details of this Theorem some technical lemmes need to be proved. An example of sequence as in (4.5) is shown in Fig.

4.]. If the error $|e(\cdot)|$ grows without then (t_k) as in (4.5) is an infinite

of. Suppose $\{t_k\}$ is a finite sequence. Then integer II exists such that $\{4.7\}$ $|o(t)| < \max\{f_0, e(t)\}$, for $t>t_H+T$.

Combining this with (4.3) we obtain, for toty+?

(4.8) $\delta(t) < -\lambda c(t) + c_0 \max (E_0, c(t))$. Inequalities (4.8), (4.7), (4.4) contradict the error growing without bounds. OED.

In the following lemms, further results are obtained when the error grows unbounded. If this is the case, an infinite sequence of instants

 $\{\xi_j\}$ exists such that $(4.9) |e(\xi_j)| = \sup_{\tau \in \mathbb{R}^n} |e(\tau)|$ $0 < |e(\xi_1)| < |e(\xi_{1+1})|$

Moreover, let us define a sequence of integers $\{k_j\}$ such that (4.10) $t_{k_j-1} \le \epsilon_j < t_{k_j}$

with (t_k) as in (4.5). n we can prove the following a 4.2. For $\{t_{k_1}\}$ as in (4.10) we can write

 $\{4.11\} \quad |\mathbf{e}(\mathbf{t}_{kj})| \geq N_0 \mathbf{e}^{-\lambda T_{kj}} |\mathbf{e}(\mathbf{\epsilon}_j)|$

for some constant $M_0>0$, λ as in (4.4) and $T_k\triangleq t_k=t_{k-1}$.

Proof. The definition of (t_k) in (4.5) implies that, for every sampling instant $(4.12) |e(t_k)| \ge e(t_k)$. Combining this with (4.3) we obtain $(4.13) |e(t_{k,j})| \ge c_0 e^{-\lambda T} k_j \int_0^{t_{k,j}} |e(\tau)| d\tau$. $(4.13) |e(t_{kj})| \ge c_0 e^{-\lambda T_{kj}}$

The adaptive gains being bounded and the error growing without bound yields the inequalities (4.14) $|\mathbf{e}(\mathbf{t})| \leq H_1 \sup_{\mathbf{t} \in \mathcal{T}} |\mathbf{e}(\mathbf{t})|$

for some positive constant My, and

$$(4.15) \int_{t_{k_{1}-1}}^{t_{k_{1}}} |e(\tau)| d\tau \ge \frac{1}{2} \min \left(\frac{1}{M_{1}}, T_{k_{1}}\right) |e(\xi_{1})|.$$

Finally, inequalities (4.13), (4.15) and $T_{k,j} \geq T$ prove the lemma.

Lemma 4.3. If the error grows without bound then the sequence $\{T_{k,j}\}$ is uniformly bounded. Proof. By equations (1.3), (2.4), (2.7) the sampled error at instant the satisfies the equation

(4.16) $e(t_{k_1}) = e^{-aT_{k_1}} e(t_{k_1-1}) - n(k_1) +$

 $e^{-aTk_j} n(k_j-1) + w(k_j) + \gamma ||\underline{\lambda}(k_j)||^2 n(k_j)$

It is shown in [12] that $\frac{(4.17) |w(k_j) + y||_{2}^{2}(k_j)||^{2} \eta(k_j)| \leq a(j)|a(\epsilon_j)|}{4.17}$ for some sequence {\$(j)} such that IIm \$(j)=0.

Furthermore, by (4.10), (4.9) and (4.11), the following inequality holds

Combining equations (4.16), (4.17), (4.18) we (4.19) $|e(z_{k_j})| \le \left[\frac{1}{k_0} e^{-(e-\lambda)^{T}k_j} + s(j) \right] |e(z_{k_j})|$

 $+ |n(k_2)| + |n(k_2-1)|$ where $\alpha - \lambda > 0$ by (4.4). By the result in (3.2), and being $|\phi(t_k)| \ge E_0 > 0$, boundedness of $T_{k,j}$ failous from inequality (4.19).

Proof of Theorem 4.2. Let us suppose the error $|\Phi(\cdot)|$ grows without bound. Then the sequence $\{k_t\}$ is in (4.10) is an infinite sequence, and labous 4.2 and 4.3 the sampled error satisfies (4.1). But Theorem 4.1 contradicts the error

growing without bound. Then i) is proved. To prove ii) suppose the sampling sequence $\{t_k\}$ to be an infinite sequence. If this is the case, by Theorem 4.1 equation (4.2) holds, which contradicts with the fact that $|a(t_k)| > E_0 > 0$ for every k. Then $\{t_k\}$ cannot be an infinite sequence. Finally iii) comes from the fact that, by ii), an instant to exist such that (4.20) $|a(t_k)| < \max_{k} (E_0, c(t))$, for every $b(t_k) < \max_{k} (E_0, c(t))$, for every $b(t_k) < \max_{k} (E_0, c(t))$, $b(t_k) < \max_{k} (E_0, c(t))$.

and then an instant $t_F \ge t^a$ exists such that (4.22) $s(t) < E_0$, for every $> t_F$ Inequalities (4.21) and (4.22) prove the last part of Theorem 4.1.

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Conclusions

An algorithm for hybrid adaptive control for single-input, single-output systems has been described.

The gains are updated at a variable rate, and the minimum time between samples can be set arbitrarily large. Uniform stability of the closed loop system is guaranteed, and the magnitude of the error can be driven smaller than an arbitrary threshold, in a finite number of adaptation. tation steps.

Nothing has been said on the performance of the algorithm in presence of disturbances and unmodeled dynamics, which is the subject of current research.

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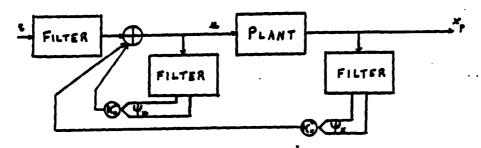


Fig 1 : Pole Placement Scheme.

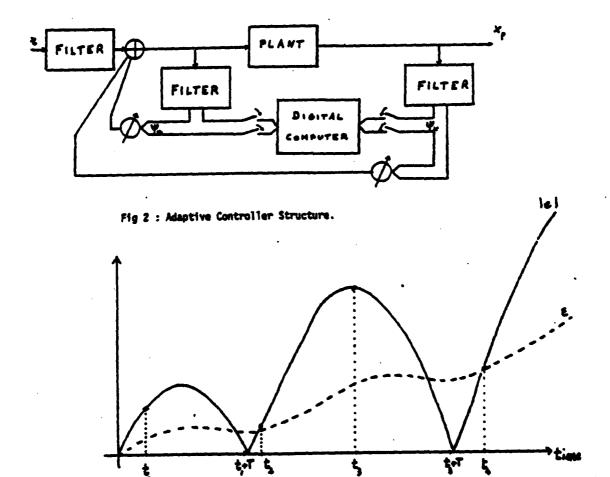


Fig 3 : Sampling Sequence.

